

Speaker : Sangtae Jeong

Title : Ergodic functions over the p-adic integers

Abstract : In this talk, we present an ergodicity criterion of a certain class of 1-Lipschitz functions on  $\mathbb{Z}_p$  for arbitrary primes  $p$ , known as  $\mathcal{B}$ -functions. These functions are locally analytic functions of order 1 (and therefore contain polynomials). For arbitrary primes  $p \geq 5$ , this ergodicity criterion leads to an efficient and practical method of constructing ergodic polynomials on  $\mathbb{Z}_p$  that realize a given unicyclic permutation modulo  $p$ . In particular, for polynomials over  $\mathbb{Z}_3$ , we provide a complete ergodicity criterion in terms of its coefficients. This method can be applied to a  $\mathbb{Z}_p$  for general primes  $p$ .